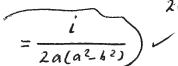
$\int_{0}^{\infty} \frac{dn}{(x^{2}+a^{2})(x^{2}+b^{2})} = \frac{1}{2} \int_{0}^{\infty} \frac{dn}{(x^{2}+a^{2})(x^{2}+b^{2})}$ Problem 36)

$$=\frac{1}{2}\int_{-\infty}^{\infty}\frac{dx}{(x+i^{2}a)(x-i^{2}a)(x+i^{2}b)(x-i^{2}b)}$$

Residue at z = ia = 2ia lia+ib)lia=ib) -



Residue at $z = ib = \frac{1}{(ib+ia)(ib-ia)zib} = \frac{i}{2b(b^2-a^2)}$

$$\int_{0}^{\infty} \frac{dx}{(x^{2}+a^{2})(x^{2}+b^{2})} = \frac{1}{2} 2\pi i \left[\frac{1}{2a(a^{2}-b^{2})} + \frac{1}{2b(b^{2}-a^{2})} \right]$$

$$=-\pi \frac{b-a}{2ab(a^2-b^2)}=\frac{\pi}{2ab(a+b)}$$

We also need to show that the integral on the Semia - Cricle goes

$$\int \frac{d^{2}}{(2^{2}+a^{2})(2^{2}+b^{2})} = \int \frac{iRe^{10}d0}{(Re^{2}i\theta_{+}a^{2})(R^{2}e^{2}i\theta_{+}b^{2})}$$
Semi-

Circle
$$\begin{cases}
\frac{1}{|R_e^{2}|^2 + a^2||R_e^{2}|^2 + b^2|} = R \int \frac{dQ}{|R_e^{2}|^2 + a^2||R_e^{2}|^2 + b^2|} = R \int \frac{dQ}{|R_e^{2}|^2 + a^2||R_e^{2}|^2 + b^2|}$$

$$\langle R \int_{0}^{T} \frac{dQ}{(R^{2}-a^{2})(R^{2}-b^{2})} = \frac{R\pi}{(R^{2}-a^{2})(R^{2}-b^{2})} \xrightarrow{R \to \infty}$$